

Dynamical equivalence of quasilinear dynamic equations on time scale

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We consider regressive and rd-continuous dynamical systems on an unbounded above and below time scale \mathbb{T} in Banach space:

$$x^\Delta = A(t)x(t) + f_1(t, x(t)), \quad (1)$$

$$x^\Delta = A(t)x(t) + f_2(t, x(t)) \quad (2)$$

where

$$|f_i(t, x) - f_i(t, x')| \leq \varepsilon(t)|x - x'|, \quad i = 1, 2,$$
$$\sup_x |f_1(t, x) - f_2(t, x)| \leq N(t) < +\infty.$$

Suppose that regressive and rd-continuous dynamical system $x^\Delta = A(t)x(t)$ has a Green type map $G(t, s)$.

Theorem 1. *If*

$$\sup_{t \in \mathbb{T}} \int_{-\infty}^{+\infty} |G(t, \sigma(s))| N(s) \Delta s < +\infty \quad (3)$$

$$\sup_{t \in \mathbb{T}} \int_{-\infty}^{+\infty} |G(t, \sigma(s))| \varepsilon(s) \Delta s = q < 1 \quad (4)$$

then dynamical systems (1) and (2) are globally dynamical equivalent.

This work was partially supported by the grant No. 345/2012 of the Latvian Council of Science.

[1] A. Reinfelds, A., Šteinberga, Dz., Dynamical equivalence of quasilinear equations, *International Journal of Pure and Applied Mathematics* 98 (2015), 355–364.